

- (d) Now, we want to get back the original unit square from the rotated square in part (b). What matrix should we use to do this? (**Note:** Don't use inverses! Answer this question using your intuition, we will visit inverses very soon in lecture!)
- (e) Use part (d) to obtain the rotation matrix that reverses the operation of a matrix that rotates a vector by θ . Multiply the reverse rotation matrix with the rotation matrix and vice-versa. What do you get?
- (f) (For practice) Next we will look at reflection matrices. The matrix that reflects about the y axis is:

$$\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

What are the matrices that reflect a vector about the (i) x -axis, and (ii) $x = y$

A natural question to ask is the following: Does the *order* in which you apply these operations matter?

- (g) Let's see what happens to a vector when we rotate it by 60° and then reflect it along the y -axis (matrix given in part (f)). Next, let's see what happens when we first reflect the vector along the y -axis and then rotate it by 60° . You will need to multiply the corresponding rotation and reflection matrices in the correct order. Are the results the same?
- (h) Now lets perform the operations in part (g) on the unit square in our iPython notebook. Are the results the same?