

#	Question	Answer(s)
1	Did we just start the lecture?	Yes there were some technical issues.
2	Can anyone else not hear anything?	live answered
3	would the norm squared of a vector - x vector work or does it have to be x vector - a vector?	Either will work. the sign difference goes away with the norm
4	What are the unknowns?	The unknowns are the 2 values in the x vector (x_1 and x_2)
5	when will mt2 scores come out?	Should be released later today.
6	why are the equations $a_1 - b_1$ and then $c_1 - a_1$. There is also a -2 in the top right but anywhere else?	It depends on how we subtract the equations. You can also factor the -2 into $(a_1 - b_1)$.
7	If all the measurements are correct, what does least square give?	It should give the correct solution to the system of equations. But this will probably make two equations linearly dependent, so we need to take care when doing the least squares. We will see it later.
8	What does Professor Waller's blue-black diagram mean?	Suppose we are working in R^3 . We measured some vector b , but and we want to find the closest vector to that b_{hat} restricted to the plane $\text{col}(A)$.
9	why do we square it?	Its generally nicer to work with norm squared, so we don't have to deal with square roots.
10	Why do we minimize e ?	e is the difference between the real b and our estimation b_{hat} , so we want to minimize it to make our estimation as good as possible.
11	we have two unknown vector here right, x_{hat} and b_{hat} ?	Yes, but we know that $A \cdot x_{\text{hat}} = b_{\text{hat}}$, and A is known. so once we know x_{hat} , we know b_{hat} .
12	Why/how does b_{hat} and b create a right triangle shouldn't they be close to parallel if they need to be similar.	We want them to be similar, but we are restricting b_{hat} to be in $\text{col}(A)$. The best we can do is if the error / difference is perpendicular to b_{hat}
13	Why do we need a separate variable b_{hat} ? Shouldn't we just use b ?	b_{hat} is our estimation of the vector b . Remember that b_{hat} can only be in the span of a , but b can be any vector.
14	Is the a vector the A matrix?	Yes in this example the A matrix only has one column, which is the a vector.
15	How do we know what's the a vector?	The a vector is basically given by the problem we want to solve. After we set up the system of equations from our measurements, we will know the a vector.
16	How can we know that the column space is a plane?	This is just part of the example. $\text{col}(A)$ is just some general subspace
17	Where did the C s come from? Why is it $c_1 a_1 + c_2 a_2 + \dots$ and not just $a_1 + a_2 + \dots$?	We know that y is in $\text{col}(A)$, so it can be written as some linear combination of the a vectors. For linear combination, we need to include those coefficient c_1, c_2, \dots since we don't know what they are
18	why is the inner product of z and the a 's equal to 0	That was part of the definitions at the beginning of the problem (it was given to us).
19	Why can't we use Gaussian Elimination to solve for x_{hat} if we have b_{hat} ?	We don't know either of them at the beginning.
20	how can the vector z be perpendicular to multiple vectors if the vectors aren't parallel	In $n \geq 3$ dimensional space it's possible. A vector perpendicular to a plane is perpendicular to any vectors in that plane. Vectors in a plane can be either parallel or not.
21	should the x in Ax have a hat on top	In this case no. We're using the identity $Ax = b + e \rightarrow e = Ax - b$
22	isn't it x_{hat} ???	On the right side, yes we should have $b = A \cdot x_{\text{hat}}$
23	Why are they (A and $b - Ax$) perpendicular?	$b - Ax = e$, the error vector. We want the best estimate for x_{hat} , so we want to minimize the norm of the error vector. That occurs when the error vector is perpendicular to $\text{col}(A)$
24	Why is b_{hat} Ax_{hat}	b_{hat} is defined by Ax_{hat} . b_{hat} is our estimation of the vector b from x_{hat} , which is our estimation of the vector x .
25	Why isn't $A_{\text{T}} \cdot A$ the identity matrix	A_{T} , the transpose, is not guaranteed to be the inverse of A . In general, it is not.
26	i thought we started by getting b_{hat}	Conceptually, we start with A and b , which are like the masks and measurements from imaging. We want to find x_{hat} and b_{hat} that gives us a best estimate.
27	why would we need to find b_{hat}	sometimes we want to check our estimation error, i.e. the difference between b and b_{hat}
28	will we be given a problem where we need to solve for the x vector even though the columns of A are linearly dependent?	such a problem is in scope
29	How many dimensions will we be asked to solve on the exam	we won't make the matrices unreasonably big for the time given
30	I thought x was supposed to be a vector? what does x being a scalar tell us?	In that example x is a scalar, or a 1×1 vector.
31	how did you get the b_{hat} equation on the left side?	$b_{\text{hat}} = A \cdot x_{\text{hat}}$. So once we have x_{hat} , its just $A \cdot x_{\text{hat}}$
32	If we use Gaussian Elimination first on a system then use the least square algorithm, will that change the result?	Yes that can change the result since Gaussian elimination will change the column space of the matrix A .
33	do we always multiply matrices from right to left?	We typically multiply from left to right, but we can also use the property $ABC = A(BC)$
34	When will we get our midterm 2 grades?	should be releasing later today
35	how did we know to do ATb to multiply to ATA^{-1} instead of ATA^{-1} multiplied to AT then b ?	You can do either. They yield the same result
36	Why is A not invertible?	In these problems, A is generally not square. So it's not invertible
37	If there is no noise will least square give us the same solution as GE and that is why we should always do least square?	Yes. The idea is the GE works when we have an exact solution. So when an exact solution exists, the "best estimate" will be the exact solution
38	do we need the system to be overdetermined for least squares to work?	yes. underdetermined systems require different algorithms
39	What happens if col of A are Lin dependent ?	Then we won't be able to execute least squares. We have to manipulate our A matrix so we can get a LI matrix
40	what would it mean if b_{hat} was exactly a , like the projection of b onto a was a , i.e $\alpha = 1$	This has no special meaning. It means the estimation $x_{\text{hat}} = 1$.
41	Kinda random, but how are orbital trajectories of planets determined now? (not by least squares right?)	The fundamentals are the same. Measure the positions, fit to a model with least squares.